



Vor 2025

Kafpróf 1 (kaflar 1 – 4)

STÆF2TE05

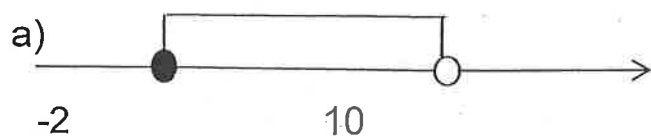
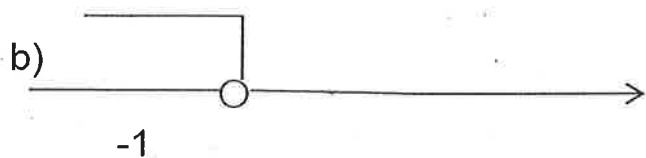
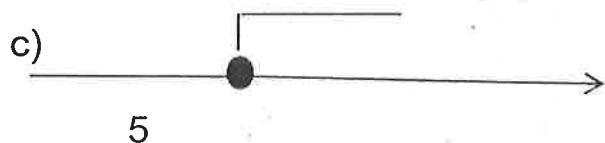
Laum

Nafn: _____ Einkunn: _____

1. (10%) Hvert er minnsta mengi (N, Z, Q eða R) sem tölugildin tilheyra til?

a) $\frac{1}{13}$ Q b) -2 Z c) $\sqrt{81}$ N d) $0,217217\dots$ Q e) π R

2. (12%) Ritaðu eftirfarandi talnabil með biltáknum:

 $[-2, 10[$  $] -\infty, -1[$  $[5, \infty[$

3. (8%) Leystu eftirfarandi ójöfnu og skilaðu svari með biltáknum:

$$2(x - 3) \geq x + 5$$

$$2x - 6 \geq x + 5$$

$$2x - x \geq 5 + 6$$

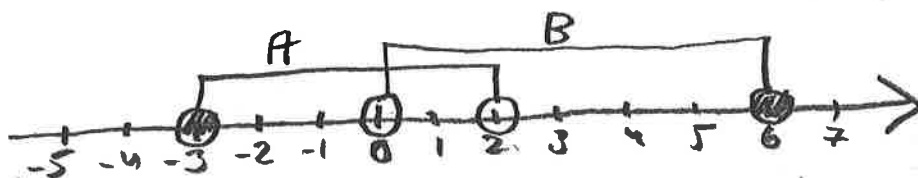
$$x \geq 11$$

 $[11, \infty[$

4. (14%) Gefin eru mengin $A = [-3, 2[$ og $B =]0, 6]$. Sýndu á talnalínu eða með biltáknum:

a) $A \cap B$

$]0, 2[$



b) $A \setminus B$

$[-3, 0]$

5. (24%) Þáttaðu eftirtaldar liðastærðir:

a) $x^2 + 13x + 30$

$(x + 3)(x + 10)$

b) $49x^2 - 4y^2$

$(7x)^2 - (2y)^2$

$(7x + 2y)(7x - 2y)$

c) $x^2 - 4x + 21$

$(x - 7)(x + 3)$

6. (16%) Reiknaðu og skilaðu sem fullstytta broti:

a) $\frac{a^3 \cdot b^2}{2x^3 \cdot b} : \frac{b^3}{4a^2 \cdot x^5}$

$$\frac{a^3 b^2}{2x^3 \cdot b} \cdot \frac{4a^2 x^5}{b^3} = \frac{\cancel{a} \cdot \cancel{a} \cdot \cancel{a} \cdot \cancel{b} \cdot \cancel{b}}{\cancel{2} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{b}} \cdot \frac{\cancel{2} \cdot \cancel{2} \cdot \cancel{a} \cdot \cancel{a} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x} \cdot \cancel{x}}{\cancel{b} \cdot \cancel{b} \cdot \cancel{b}}$$

$$= \frac{2a^5 x^2}{b^2}$$

b) $\frac{x^2 - 8x + 12}{4x^2 - 16} : \frac{(x-2)(x-6)}{4(x+2)(x-2)}$

$$\frac{x-6}{4(x+2)}$$

7. (16%) Einfaldaðu eftirfarandi algebrubrot:

a) $\frac{3x}{4} + \frac{2x}{3} - \frac{x}{12}$

$$\frac{3x \cdot 3}{4 \cdot 3} + \frac{2x \cdot 4}{3 \cdot 4} - \frac{x \cdot 1}{12 \cdot 1} = \frac{9x}{12} + \frac{8x}{12} - \frac{x}{12} = \frac{9x + 8x - x}{12} = \frac{16x}{12}$$

$$= \frac{4x}{3}$$

b) $\frac{x}{4} - \frac{(x+2)}{(x-1)}$

$$\frac{x(x-1)}{4(x-1)} - \frac{4(x+2)}{4(x-1)}$$

$$\frac{x(x-1) - 4(x+2)}{4(x-1)} = \frac{x^2 - x - 4x - 8}{4(x-1)} = \frac{x^2 - 5x - 8}{4(x-1)}$$