

Afleiður nokkurra falla

Diffrunarreglur

$f(x) = x^n$	$f'(x) = nx^{n-1}$		
$f(x) = \sqrt{x}$	$f'(x) = \frac{1}{2\sqrt{x}}$	$y = k \cdot f(x)$	$y' = k \cdot f'(x)$
$f(x) = \sin(x)$	$f'(x) = \cos(x)$	$y = f(x) + g(x)$	$y' = f'(x) + g'(x)$
$f(x) = \cos(x)$	$f'(x) = -\sin(x)$	$y = f(x) \cdot g(x)$	$y' = f'(x) \cdot g(x) + f(x) \cdot g'(x)$
$f(x) = \tan(x)$	$f'(x) = \frac{1}{\cos^2(x)}$	$y = \frac{f(x)}{g(x)}$	$y' = \frac{f'(x)g(x) - f(x)g'(x)}{g^2(x)}$
$f(x) = \tan(x)$	$f'(x) = 1 + \tan^2(x)$	$y = f(g(x))$	$y' = f'(g(x)) \cdot g'(x)$
$f(x) = \cot(x)$	$f'(x) = -(1 + \cot^2(x))$	$f(x) = \cot(x)$	$f'(x) = \frac{-1}{\sin^2(x)}$
$f(x) = \ln(x)$	$f'(x) = \frac{1}{x}$	Reglur um diffur	
$f(x) = \log_a(x)$	$f'(x) = \frac{1}{x \cdot \ln(a)}$		
$f(x) = e^x$	$f'(x) = e^x$	$d(f \cdot g) = df \cdot g + f \cdot dg$	$d\left(\frac{f}{g}\right) = \frac{df \cdot g - f \cdot dg}{g^2}$
$f(x) = a^x$	$f'(x) = a^x \ln(a)$	$d(f \pm g) = df \pm dg$	$d(f(g(x))) = f'(g(x)) \cdot dg(x)$
$f(x) = \arcsin(x)$	$f'(x) = \frac{1}{\sqrt{1-x^2}}$	Línuleg nálgun	
$f(x) = \arctan(x)$	$f'(x) = \frac{1}{1+x^2}$		
$l(x) = f(x_0) + f'(x_0)(x - x_0)$			

Stofnföll nokkurra falla

$\int x^n dx = \frac{x^{n+1}}{n+1} + K$	$\int \sin(x) dx = -\cos(x) + K$	$\int \cos(x) dx = \sin(x) + K$
$\int (1 + \tan^2(x)) dx = \tan(x) + K$	$\int (1 + \cot^2(x)) dx = -\cot(x) + K$	$\int \frac{1}{a^2 + b^2 x^2} dx = \frac{1}{ab} \arctan\left(\frac{bx}{a}\right) + K$
$\int \tan^2(x) dx = \tan(x) - x + K$	$\int \cot^2(x) dx = -\cot(x) - x + K$	$\int \frac{1}{\sqrt{a^2 - b^2 x^2}} dx = \frac{1}{b} \arcsin\left(\frac{bx}{a}\right) + K$
$\int e^x dx = e^x + K$	$\int a^x dx = \frac{a^x}{\ln(a)} + K$	$\int \frac{1}{x} dx = \ln x + K$

Heildunarreglur

$\int f(x) dx = F(x) + K, \quad F'(x) = f(x)$	$\int_a^b f(x) dx = [F(x)]_a^b = F(b) - F(a)$
$\int k \cdot f(x) dx = k \int f(x) dx$	$\int_a^b k \cdot f(x) dx = k \int_a^b f(x) dx$
$\int (-f(x)) dx = -\int f(x) dx$	$\int_a^a f(x) dx = 0$
$\int (f(x) + g(x)) dx = \int f(x) dx + \int g(x) dx$	$\int_a^b f(x) dx = -\int_b^a f(x) dx$
$\int_a^b f(x) dx = f(c)(b-a)$	$\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$

Flatarmál – Rúmmál

$A = \int_a^b f(x) dx = [F(x)]_a^b$	$A = \int_a^b (f(x) - g(x)) dx = \int_a^b (EF - NF) dx$
$V = \int_a^b \pi (f(x))^2 dx = \int_a^b \pi \cdot R^2 dx$	$V = \int_a^b \pi ((f(x))^2 - (g(x))^2) dx = \int_a^b \pi \cdot (R^2 - r^2) dx$

Heildunaraðferðir

$$\int f(g(x)) \cdot g'(x) dx = \int f(t) dt = F(t) + K = F(g(x)) + K$$

$t = g(x) \quad \text{og} \quad dt = g'(x) dx$

$$\int f \cdot dg = fg - \int g \cdot df$$

$$\int_a^b f(g(x)) \cdot g'(x) dx = \int_{g(a)}^{g(b)} f(t) dt = [F(t)]_{g(a)}^{g(b)}$$

$t = g(x) \quad x = b, \quad t = g(b)$
 $dt = g'(x) dx \quad x = a, \quad t = g(a)$

$$Ax^2 + Bx + C = 0$$

$$D = B^2 - 4AC$$

$$x = \frac{-B \pm \sqrt{D}}{2A}$$

Diffurjöfnur

$\frac{dy}{dx} = f(x)$ $y = F(x) + K$	$\frac{dy}{dx} = f(x) \cdot g(y) \Rightarrow$ $\int \frac{1}{g(y)} dy = \int f(x) dx$	$y' + f(x)y = g(x)$ $y = e^{-F(x)} \int g(x)e^{F(x)} dx$
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Reiknireglur logra

$\ln(ab) = \ln(a) + \ln(b)$	$\ln\left(\frac{a}{b}\right) = \ln(a) - \ln(b)$	$\ln(a^n) = n \ln(a)$	$\ln(1) = 0$ $\ln(e) = 1$	$\log_a(x) = \frac{\ln(x)}{\ln(a)}$
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Andhverf hornaföll

$\sin(\arcsin(x)) = x$	$\cos(\arccos(x)) = x$	$\tan(\arctan(x)) = x$	$\cot(\text{arccot}(x)) = x$
$\arcsin(\sin(x)) = x$	$\arccos(\cos(x)) = x$	$\arctan(\tan(x)) = x$	$\text{arccot}(\cot(x)) = x$
$\arcsin(-x) = -\arcsin(x)$	$\arccos(-x) = \pi - \arccos(x)$	$\arctan(-x) = -\arctan(x)$	$\text{arc cot}(-x) = -\text{arc cot}(x)$
$\arcsin(x) + \arccos(x) = \frac{\pi}{2}$	$\arctan(x) + \text{arc cot}(x) = \frac{\pi}{2}$		

	$y = \arcsin(x)$	$y = \arccos(x)$	$y = \arctan(x)$	$y = \text{arccot}(x)$
Skilgr.mengi	$-1 \leq x \leq 1$	$-1 \leq x \leq 1$	$-\infty < x < \infty$	$-\infty < x < \infty$
Myndmengi	$-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$	$0 \leq y \leq \pi$	$-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$	$0 < y < \pi$

Summur - Runur - Raðir

$\sum_{i=k}^n a_i = a_k + a_{k+1} + \dots + a_n$	Runa $\{a_i\} = a_1, a_2, a_3, \dots, a_i, \dots$	Röð $\sum_{i=1}^{\infty} a_i = a_1 + a_2 + a_3 + \dots$
$s_j = \sum_{i=1}^n k_i \cdot \Delta x_i$	$S_j = \sum_{i=1}^n K_i \cdot \Delta x_i$	$\sigma_j = \sum_{i=1}^n f(t_i) \cdot \Delta x_i$

Mismunaruna $\{a_i\}$

$a_{i+1} = a_i + d$	$a_i = a_1 + (i-1)d$	$s_n = n \cdot \frac{a_1 + a_n}{2}$	$s_n = n \cdot \frac{2a_1 + (n-1)d}{2}$
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Kvótaruna $\{a_i\}$

$a_{i+1} = a_i \cdot q$	$a_i = a_1 \cdot q^{i-1}$	$s_n = a_1 \cdot \frac{1 - q^n}{1 - q}$
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