

Hornafræði

Skilgreiningar

Sínus: $\sin(v)$

Cosínus: $\cos(v)$

Tangens: $\tan(v)$

Cotangens: $\cot(v)$

$$\cos(v) = \frac{\text{aðlæg hlið}}{\text{langhlið}} = \frac{b}{c}$$

$$\sin(v) = \frac{\text{mótlæg hlið}}{\text{langhlið}} = \frac{a}{c}$$

$$\tan(v) = \frac{\text{mótlæg hlið}}{\text{aðlæg hlið}} = \frac{a}{b} = \frac{1}{\cot(v)}$$

Umskriftarreglur

$$\sin(v+360^\circ h) = \sin(v)$$

$$\cos(v+360^\circ h) = \cos(v)$$

$$\tan(v+180^\circ h) = \tan(v)$$

$$\cot(v+180^\circ h) = \cot(v)$$

$$\sin(180^\circ - v) = \sin(v)$$

$$\cos(180^\circ - v) = -\cos(v)$$

$$\tan(180^\circ - v) = -\tan(v)$$

$$\cot(180^\circ - v) = -\cot(v)$$

$$\sin(360^\circ - v) = -\sin(v)$$

$$\cos(360^\circ - v) = \cos(v)$$

$$\tan(360^\circ - v) = -\tan(v)$$

$$\cot(360^\circ - v) = -\cot(v)$$

$$\sin(v+180^\circ) = -\sin(v)$$

$$\cos(v+180^\circ) = -\cos(v)$$

$$\tan(v+180^\circ) = \tan(v)$$

$$\cot(v+180^\circ) = \cot(v)$$

$$\sin(-v) = -\sin(v)$$

$$\cos(-v) = \cos(v)$$

$$\tan(-v) = -\tan(v)$$

$$\cot(-v) = -\cot(v)$$

$$\sin^2(v) + \cos^2(v) = 1$$

Lausn á hornafallajöfnu

$$\sin(v) = k$$

$$\cos(v) = k$$

$$\tan(v) = k$$

$$v = \begin{cases} \sin^{-1}(k) \\ 180 - \sin^{-1}(k) \end{cases}$$

$$v = \begin{cases} \cos^{-1}(k) \\ -\cos^{-1}(k) \end{cases}$$

$$v = \tan^{-1}(k)$$

Flatarmál þríhyrnings $F = \frac{1}{2} \cdot b \cdot c \cdot \sin(A)$

Sínusreglan	$\frac{a}{\sin(A)} = \frac{b}{\sin(B)} = \frac{c}{\sin(C)}$	Cosínusreglan	$a^2 = b^2 + c^2 - 2 \cdot b \cdot c \cdot \cos(A)$
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v (rad)	0	$\pi/6$	$\pi/4$	$\pi/3$	$\pi/2$
v° (gráður)	0	30°	45°	60°	90°
sin(v)	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
cos(v)	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0
tan(v)	0	$\frac{\sqrt{3}}{3} = \frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	óskilgr.
cot(v)	óskilgr.	$\sqrt{3}$	1	$\frac{\sqrt{3}}{3} = \frac{1}{\sqrt{3}}$	0